

## Abstract

Let  $\mathcal{A} = \{H_1, \dots, H_l\}$  be a hyperplane arrangement in  $\mathbb{C}^n$  and  $M$  be the complement of the union of hyperplanes in  $\mathcal{A}$ , i.e.,  $M = \mathbb{C}^n \setminus \bigcup_{i=1}^l H_i$ . The cohomology algebra  $H^*(M, \mathbb{C})$  has a complete combinatorial description. Let  $\mathcal{L}$  be a local system on  $M$  and  $H^*(M, \mathcal{L})$  be the cohomology algebra with local coefficients. For  $[\omega] \in H^1(M, \mathbb{C})$ , there is a chain complex:

$$0 \rightarrow H^0(M, \mathbb{C}) \xrightarrow{\mu_\omega} H^1(M, \mathbb{C}) \xrightarrow{\mu_\omega} \dots \xrightarrow{\mu_\omega} H^n(M, \mathbb{C}) \rightarrow 0.$$

The characteristic varieties of  $M$  are the jumping loci of the cohomology groups  $H^*(M, \mathcal{L})$ . The resonance varieties of  $M$  are the jumping loci of the cohomology groups of the above complex. The aim of this thesis is to study some properties of these varieties.