

# Abstract

Let  $\Gamma'' = [V(\Gamma''), E(\Gamma'')]$  be a graph with set of vertices and edges  $V(\Gamma'')$  and  $E(\Gamma'')$  respectively such that,  $|V(\Gamma'')|$  is order and  $|E(\Gamma'')|$  is size of the graph  $\Gamma''$ . Let  $G''$  be a group and  $A \subseteq G''$  be a subset of the group  $G''$ . The commuting graph  $\Gamma'' = [G'', A]$  of the group  $G''$  is a graph with vertex-set  $V(\Gamma'') = A$  such that two distinct vertices  $x, y \in V(\Gamma'')$  are connected by an edge i.e  $xy \in E(\Gamma'')$  iff  $xy = yx$  in  $G''$ . In this thesis, we study the certain properties of the commuting graph on Dicyclic group

$$D_n^{**} = \langle a, x : a^{2n} = 1, x^2 = a^n, a^x = a^{-1} \rangle$$

of order  $4n$  and construct different families of graphs. In addition, we also obtain the certain parameters of graph theory such as chromatic number, clique number and perfect matching.